

Recap:-

Landauer Buttiker approach

~10 mins → # Ohm's law like behaviour

Landauer Buttiker approach

$G^{-1} \rightarrow$ calculated for different regimes

Buttiker Formula / Landauer + Buttiker

$$I = \frac{2e}{h} F(u_1, u_2)$$

Two terminal

$$I_p = \frac{2e}{h} \sum_q T_{q \leftarrow p} u_p - T_{p \leftarrow q} u_q$$

$$I_p = \sum_q [G_{qp} V_p - G_{pq} V_q]$$

$$G_{pq} = \frac{2e^2}{h} T_{p \leftarrow q}$$

Current Conservation

$$\sum_q G_{pq} = \sum_q G_{qp}$$

not as cool?

⇒ Datta's book → Buttiker formula

$T_{q \leftarrow p}$: transmission for mode going from p to q .

$$I_p = \sum_q [G_{qp} V_p - G_{pq} V_q]$$

$G_{pq} = \frac{2e^2}{h}$ pairwise conductance from p to q .

$I = \frac{2e}{h} F(u_1, u_2)$

Two terminal

$$I_p = \frac{2e}{h} \sum_q T_{q \leftarrow p} u_p - T_{p \leftarrow q} u_q$$

$$I_p = \sum_q [G_{qp} V_p - G_{pq} V_q]$$

$$G_{pq} = \frac{2e^2}{h} T_{p \leftarrow q}$$

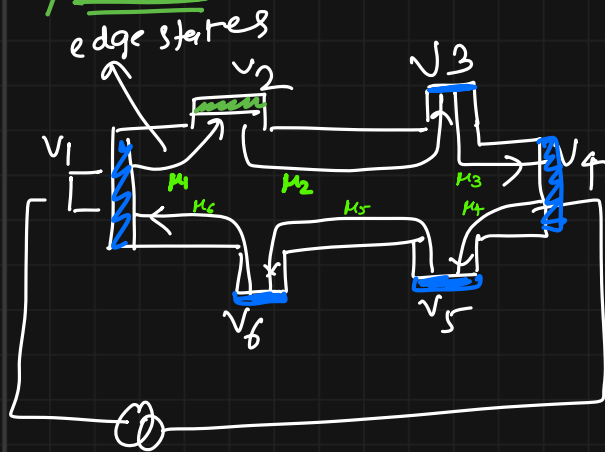
Current Conservation

$$\sum_q G_{pq} = \sum_q G_{qp}$$

$$I_p = \sum_q G_{pq} [V_p - V_q]$$

allows us to get different terminal currents (???)

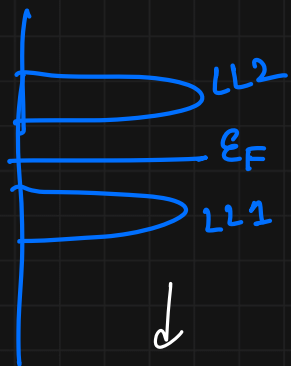
problems:- can be found in Datta's book



$\phi_{Hall} \rightarrow$ edge states

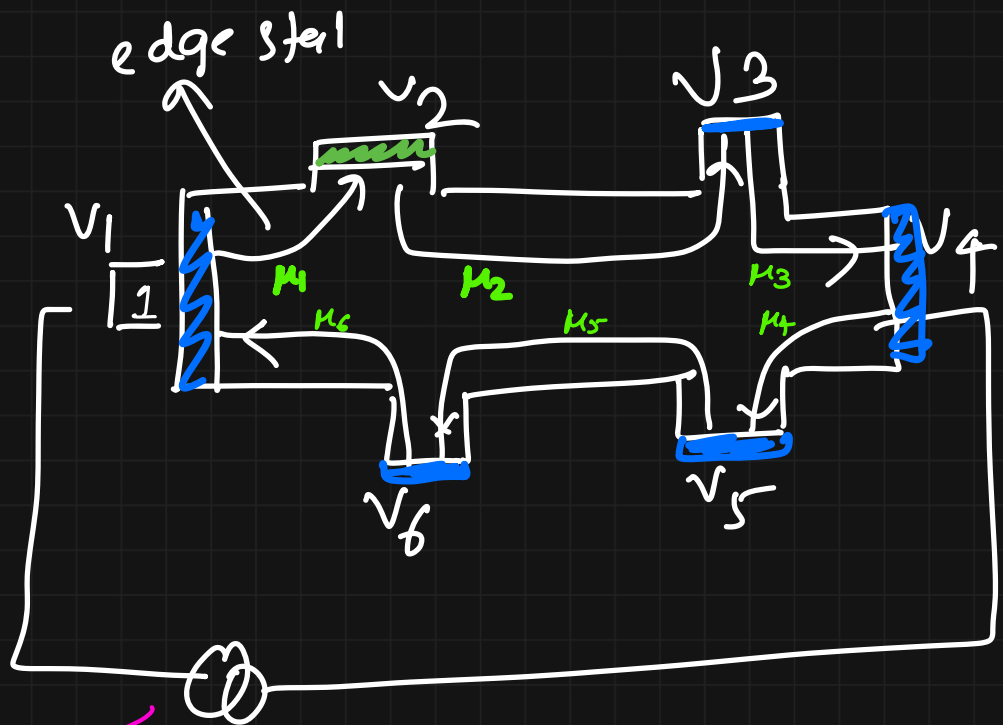
$\therefore$ no net current flow in this Geometry.

metal contact equilibrates an arriving electron

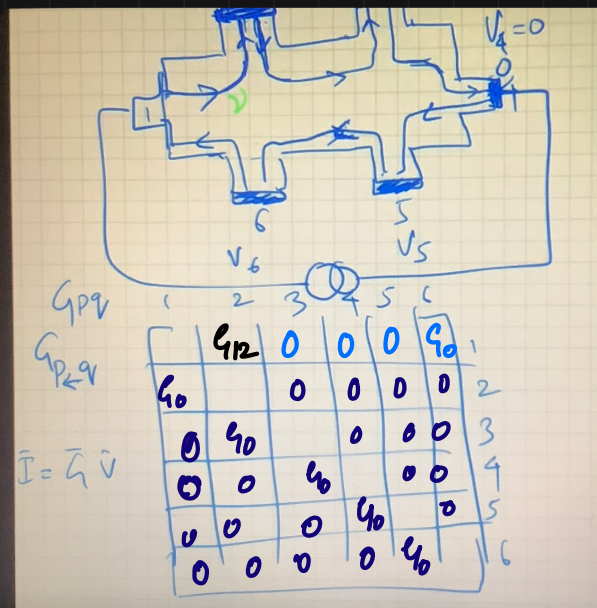


bulk will have edge states & backscatter.
 $\Rightarrow$ we conveniently take

Current source



Current cons:- $\sum_{row} \text{ or } \sum_{column} = 0$



$G_{12} \leftarrow$ transmission from electrode 2 to 1.

$\hookrightarrow$ edge states $\rightarrow$ chiral

$G_{12} = 0 \rightarrow$ since no states

$G_{matrix} > 0$ go from ② to ①

take only direct transmission

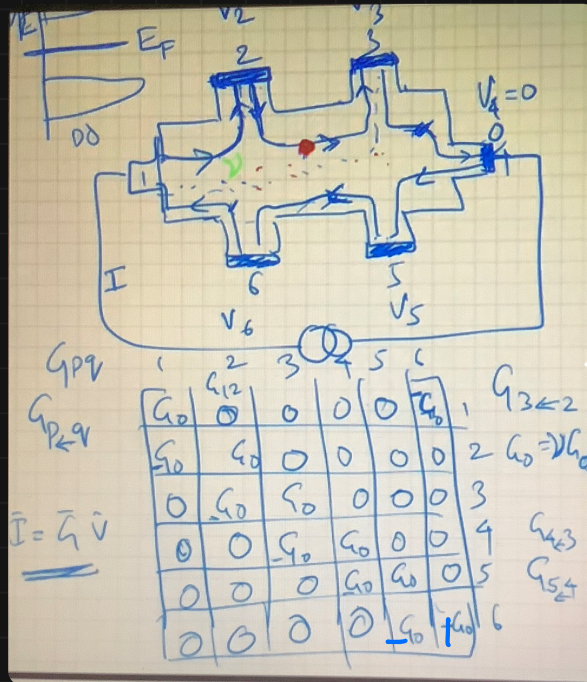
$$G_0 = v \left(\frac{2e^2}{h} \right)$$

v = filling factor

Quantum of conductance

$$G_{65} = G_{6 \leftarrow 5}$$

To get current cons, make all row sums & column summations to be 0.



we conserve the current by flipping the sign on an off diagonal element (just a convention)

$$\begin{pmatrix} 2 \\ 0 \\ 0 \\ -2 \\ 0 \\ 0 \end{pmatrix} = \begin{pmatrix} | & | & | & | & | & | \\ | & | & | & | & | & | \\ | & | & | & | & | & | \\ | & | & | & | & | & | \\ | & | & | & | & | & | \\ | & | & | & | & | & | \end{pmatrix} \begin{bmatrix} V_1 \\ V_2 \\ V_3 \\ V_4 = 0 \\ V_5 \\ V_6 \end{bmatrix}$$

send current here (pointing to the 2 in the vector)

take it out here (pointing to the -2 in the vector)

omit 4th row & column (pointing to the 4th row and column of the matrix)

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simple hell bar 2021.nb - Wolfram Mathematica 12.1
File Edit Insert Format Cell Graphics Evaluation Palettes Window Help

In[ ]:=
mat = {{g, 0, 0, 0, 0, -g}, {-g, g, 0, 0, 0, 0}, {0, -g, g, 0, 0, 0}, {0, 0, -g, g, 0, 0}, {0, 0, 0, -g, g, 0}, {0, 0, 0, 0, -g, g}};
Out[ ]:= {{g, 0, 0, 0, 0, -g}, {-g, g, 0, 0, 0, 0}, {0, -g, g, 0, 0, 0}, {0, 0, -g, g, 0, 0}, {0, 0, 0, -g, g, 0}, {0, 0, 0, 0, -g, g}}

In[ ]:= MatrixForm[mat]
Out[ ]:= MatrixForm[
  g  0  0  0  0 -g
 -g  g  0  0  0  0
  0 -g  g  0  0  0
  0  0 -g  g  0  0
  0  0  0 -g  g  0
  0  0  0  0 -g  g

In[ ]:= geff = Drop[mat, {4}, {4}]
Out[ ]:= {{g, 0, 0, 0, -g}, {-g, g, 0, 0, 0}, {0, -g, g, 0, 0}, {0, 0, -g, g, 0}, {0, 0, 0, -g, g}}

In[ ]:= Inverse[geff]
Out[ ]:= {{1/g, 0, 0, 0, 1/g}, {1/g, 1/g, 1/g, 1/g, 1/g}, {0, 0, 1/g, 0, 0}, {0, 0, 0, 1/g, 0}, {0, 0, 0, 0, 1/g}}
  
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we want to find other voltages

$\nu_{23} \rightarrow 0$ longitudinal resistance = 0

hall mark of Hall effect

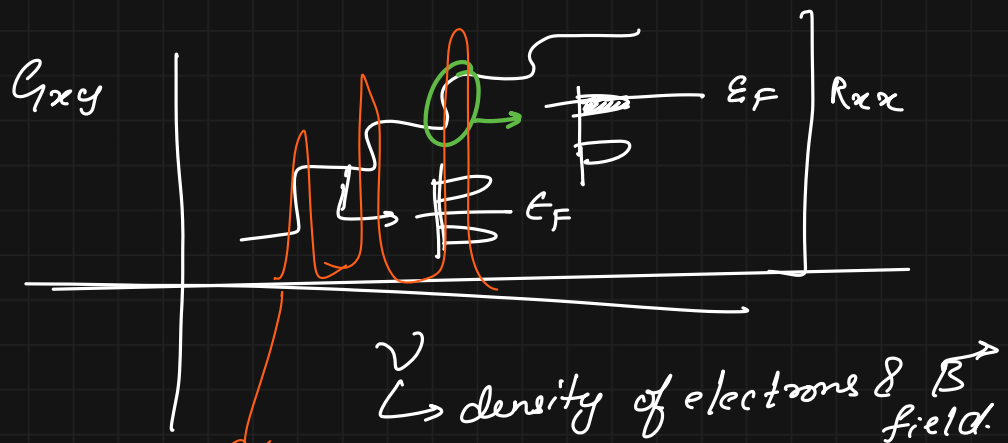
ν_{Hall} hall mark $\rightarrow$ transverse voltage

related to conductance $\leftarrow$ drop is same & related to filling factors

$\Rightarrow$ no backscattering $\rightarrow$ # of channels are same
 $\therefore$ conductance is same

X no density gradient $\rightarrow$ magnetic field has to be uniform.

$\Rightarrow E_F$ b/w L. levels, then things are complicated.



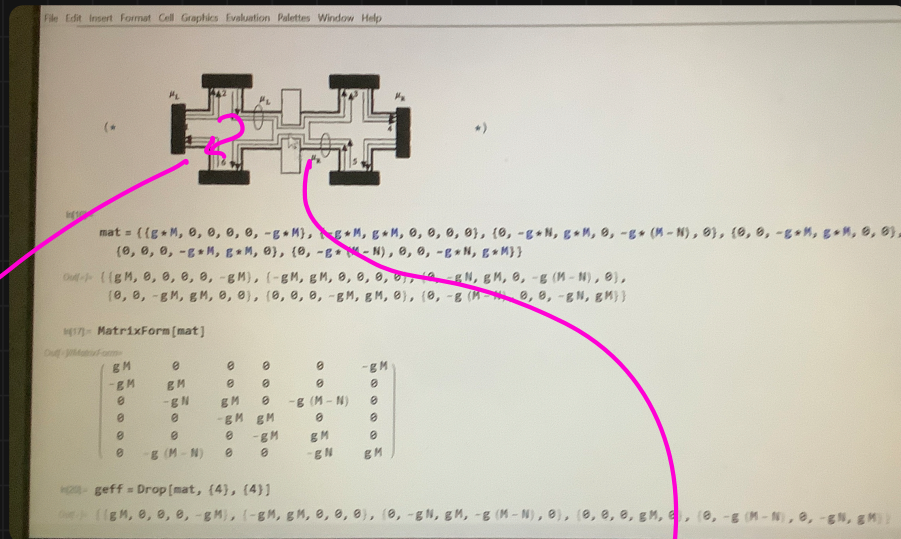
R_{xx}
= backscattering allowed
resistance

$\rightarrow$ exponentially goes to zero

Note:- We currently work at 0 Temp.

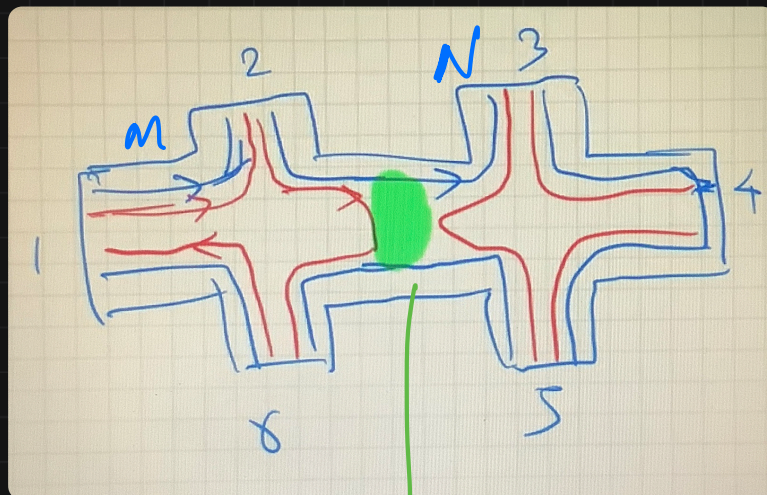
In 2D, resistance $\rightarrow$ conductance matrix transf.'s
 $\downarrow$ tricky
 $T_{xx} \rightarrow 0$ in b/w the londane levels

Example 2:-

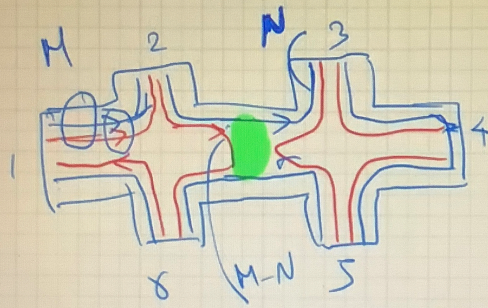


few edge modes shall get reflected

charge density is different



region of non-uniform density



1 2 3 4 5 6

G_{12}

	1	2	3	4	5	6	
	0	0	0	0	0	G_M	1
G_M		0	0	0	0	0	2
0	NG_0		0	$G_0(MN)$	0	0	3
0	0	MG_0		0	0	0	4
0	0	0	MG_0		0	0	5
0	$M-N$	0	0	NG_0		0	6

